



Planning a geostatistical survey to map soil and crop properties: eliciting sampling densities

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Abstract. The communication of uncertainty is not only a challenge when soil information has been produced but also in the planning stage. When planning a survey of soil properties it is necessary to make decisions about the sampling density. Sampling density determines both the quality of predictions and the cost of fieldwork. In this study, we considered four ways in which the relationship between sample density and the uncertainty of predictions can be related, based on prior information

- 5 about the variability of the target quantity. These were offset correlation, prediction intervals, conditional probabilities of the interpretation errors and implicit loss functions. Offset correlation is a measure of the consistency of kriging predictions made from sample grids with the same spacing but different origins. Prediction intervals and conditional probabilities are based on the prediction distribution of the variable of interest. All four of these methods were investigated using information on soil pH and Se concentration in grain in Malawi. They were presented to a group of stakeholders, who were asked to use them
- 10 in turn to select a sampling density. Their responses were evaluated and they were then asked to rank the methods based on their effectiveness, in their experience, and in terms of finding a level of uncertainty that they were able to tolerate when deciding about a sampling grid spacing. Our results show that the approach that stakeholders favoured was offset correlation, and some approaches were not well understood (conditional probability and implicit loss function). During feedback sessions, the stakeholders highlighted that they were more familiar with the concept of correlation, with a closed interval of [0,1] and
- 15 this explains the more consistent responses under this method. The offset correlation will likely be more useful to stakeholders, with little or no statistical background, who are unable to express their requirements of information quality based on other measures of uncertainty.

1 Introduction

Micronutrient deficiencies (MND) are a widespread health problem in sub-Saharan Africa (Hurst et al., 2013; Joy et al., 2014;
Phiri et al., 2019). In the GeoNutrition project, it has been shown that concentration of micronutrients in staple crops and in soils vary spatially and so interventions to address the deficiencies should be based on spatial information (Gashu et al., 2021;



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Botoman et al., 2022). In our previous studies (Chagumaira et al., 2021, 2022) we have shown that geostatistical predictions can help stakeholders to make decisions for interventions to address MND, by accounting for uncertainty in the supporting information which has been produced by statistical prediction from data and covariates. Spatial information is obtained from surveys, and in most cases, budgets for surveys are limited and the stakeholders involved may have different set of questions to address and common ground is often difficult to establish. Often surveys efforts are constrained by budgets and we need a trade-off between sample effort and reducing uncertainty. This requires that stakeholders, who must decide on sampling budgets, can understand the relationship between effort, hence cost, and uncertainty.

When planning a survey of soil properties it is necessary to make decisions about the sampling density (e.g. de Gruijter et al.,
2006; Webster and Lark, 2013). Sampling density determines both the quality of predictions and the cost of field work. It is possible to draw some conclusions about spatial variation to support decisions on subsequent sampling from an approximate variogram of a region (Lark et al., 2017). In geostatistical prediction, the variogram function models the spatial dependence of the variable of interest, and the uncertainty in the predicted values in quantified by the kriging variance (i.e., the mean squared error of the prediction). Therefore, if we have a reasonable estimate of variance parameters (i.e. variogram for ordinary)

- 35 kriging) we can compute kriging variances for different grid spacings and, in principle, select an acceptable one (McBratney et al., 1981). In cases where we do not know the variogram (as we have yet to sample), a variogram from comparable regions can be used instead to provide estimates of variance parameters (Alemu et al., 2022). Alternatively, an approximate variogram from a reconnaissance study, accounting for uncertainty e.g., by a Bayesian approach, can be used to provide reasonable estimates of variance parameters (Lark et al., 2017). An estimate of variance parameters can be obtained through an average
- 40 variogram or some other generalised model extracted from published studies (Paterson et al., 2018), or a variogram elicited from experts (Truong et al., 2013).

Kriging variances are a direct measure of uncertainty resulting from the prediction model. The kriging variance, at some location, depends only on the variogram and the spatial distribution of observations (Webster and Oliver, 2007; Webster and Lark, 2013). As the sampling density increases around a location, then the kriging variance diminishes. Because field and

- 45 analytical costs increase in parallel with sampling density, the kriging variance, as a measure of the resulting uncertainty, could be used to find an appropriate sample density such that the information user is satisfied with the trade off between cost and the quality of information. However, kriging variance is not an accessible measure of uncertainty for many end users (Chagumaira et al., 2021), and so it is likely that other methods of communicating the implications of sampling density on uncertainty would be better.
- 50 Kriging is unbiased, and on the assumption of normality of the kriging errors, prediction intervals can be computed from kriging variances. Prediction intervals reflect the spatial variability of the variable and density of the samples (Webster and Oliver, 2007). However, we know that prediction intervals are not preferred by end-users as a method of communicating uncertainty when making decisions, they find it easier to interpret measures of uncertainty tied to a particular decisions (Chagumaira et al., 2021). For example, the probability that the value of a soil property at some location does not exceed a threshold, below
- 55 which some intervention is needed. However, the kriging variance and prediction interval give measures of uncertainty but do not contextualise them with respect to the decision being made. If the purpose of the survey is to support decisions about





a certain intervention then it may be useful for the end-user to understand the implications of sampling in terms of the risk that the resulting information leads to incorrect decisions in particular situations. This can be considered as a general, decision related uncertainty measure.

- We may consider some sampling design (e.g. square grid) and a notional unsampled location, \mathbf{x}_0 , at which information is needed to support a decision. For a conservative measure of uncertainty, \mathbf{x}_0 , may be at a general location where uncertainty is largest e.g, at the centre of a square grid cell. We may then compute, over a specified distribution of the target variable, the probability that the predicted value of the property will indicate that no intervention is required at \mathbf{x}_0 conditional on the true value, $Z(\mathbf{x}_0)$, indicating that actually an intervention is needed. That is to say, the probability that the spatial information
- 65 will fail to indicate the correct decision at sites where a management or policy intervention is required. This probability will depend on the specific statistical model for the variable but also on sampling density. The conditional probabilities can then be used to make a decision about soil sampling, by selecting an appropriate grid spacing which limits the risk to acceptable level. Conditional probabilities have not been used in this way before, but there might be a way to tie uncertainty to a specific decision in a way which will help the stakeholder to understand its significance.
- A further way to develop the decision-focussed approach to sample planning is to consider the costs of sampling and the costs resulting from uncertainty. This requires the data user's loss function. A loss function expresses the costs incurred resulting from using erroneous information to make a decision for an intervention (Goovaerts, 1997). The loss function determines the expected loss when the prediction is used to make a decision. We can then compute the expected loss for a decision as a function of the precision of supporting information which in turn depends on the sampling density, and compare this with the
- 75 cost of obtaining sample data with that density. It may not be possible to define a loss function prior to making decisions on soil sampling strategy because the cost of the errors are difficult to frame and quantify. However, an implicit loss function, conditional on a logistical model (i.e. a function of sampling effort and statistical information about the estimates of the cost of errors) can be modelled as the loss function that makes a particular decision on sampling effort rational (Lark and Knights, 2015). The logistical model can be obtained from data from a previous survey or a from a comparable region. Lark and Knights
- 80 (2015) suggested that reflection on the implicit loss function for different sample schemes, or competing projects, may help decision-makers to arrive at loss functions which might be regarded as plausible.

Decisions on soil sampling can be based on more general measures of uncertainty, that relate to sampling intensity, such as the offset correlation (Lark and Lapworth, 2013). The offset correlation is a measure of the robustness of the resulting map to arbitrary variation in the location of the origin of a fixed regular sampling grid. For example, the offset correlation increases

as the uncertainty in the map, attributable to sample density, decreases. It is not directly related to the decision process but dependent on the variogram and the proposed sampling spacing. The offset correlation might be a more intuitive uncertainty measure than prediction intervals and kriging variances. This is because people can more easily grasp and evaluate bounded measures such as the correlation (Hsee, 1998).

In this study we aimed to find out whether groups of stakeholders were able to make decisions on soil and crop sampling 90 strategies, in particular sampling density using soil pH and selenium concentration in grain (Se_{grain}), with the methods de-





scribed above. We aimed to address the following questions: (i) *can stakeholders use the different approaches consistently?* (ii) *do the stakeholders have a preference?* and (iii) *does their use/preference depend on their background and experience?* In the next section of this paper, we describe in detail the test approaches.

2 Theory

95 2.1 Prediction interval

Some unknown quantity at a location (e.g. soil pH or Se_{grain}) is characterised by a prediction distribution conditional on the data and statistical model. The kriging variance at the unsampled location, x_0 , is defined as

$$\sigma_{\rm K}^2 = {\rm E}[\{Z(\mathbf{x}_0) - \tilde{Z}(\mathbf{x}_0)\}^2],\tag{1}$$

where $\tilde{Z}(\mathbf{x}_0)$ is a prediction of the random variable $Z(\mathbf{x}_0)$. The kriging prediction is a weighted average of the data

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$$\tilde{Z}(\mathbf{x}_0) = \sum_{i=1}^N \lambda z(\mathbf{x}_0),$$
 (2)

where $z(\mathbf{x}_0)$ is the data and λ are the kriging weights (Webster and Oliver, 2007). The kriging variance, σ_K^2 is defined as:

$$\sigma_{\rm K}^2 = {\rm E}[\{Z(\mathbf{x}_0) - \tilde{Z}(\mathbf{x}_0)\}^2].$$
(3)

Cross-validation predictions of the statistical model need to be examined by exploratory analysis of the kriging error, $\varepsilon(\mathbf{x}_0) = \{z(\mathbf{x}_0) - \tilde{Z}(\mathbf{x}_o)\}$ to check if the assumption of the normality holds. The kriging predictor is unbiased and the mean of the errors 105 is zero, and their standard deviation is equal to the kriging standard deviation, σ_K , from kriging. Based on this, a 95% prediction interval can be computed as:

 $\left[\tilde{Z}(\mathbf{x}_0) - 1.96\sigma_{\mathrm{K}}(\mathbf{x}_0), \tilde{Z}(\mathbf{x}_0) + 1.96\sigma_{\mathrm{K}}(\mathbf{x}_0)\right].$ (4)

The prediction distribution may also be obtained on a block support–for example if predictions are required at the scale of a farm mean or a mean for an administrative region. The same approach holds to the derivation of a prediction interval.

110 2.2 Conditional probability

We can calculate the joint probability that a location requires an intervention, and that the kriged estimate does not indicate this. If \mathbf{x}_0 is the location of interest, $\tilde{Z}(\mathbf{x}_o)$ is the prediction and $z(\mathbf{x}_0)$ the value of the variable at \mathbf{x}_0 , then $\tilde{Z}(\mathbf{x}_o) - z(\mathbf{x}_0) = \varepsilon(\mathbf{x}_0)$, the error of the kriging predictions. The covariance of $z(\mathbf{x}_0)$ and $\varepsilon(\mathbf{x}_0)$ is:





$$\operatorname{Cov}\left[\mathbf{z}(\mathbf{x}_{0}), \varepsilon(\mathbf{x}_{0})\right] = \operatorname{Var}\left[\mathbf{Z}(\mathbf{x}_{0})\right] - \boldsymbol{\lambda}^{\mathrm{T}} \mathbf{c},\tag{5}$$

115 where λ denotes the vector of kriging weights for observations used to make the prediction, and c denotes the vector of covariances between each of these observations and $Z(\mathbf{x}_0)$. We can therefore, specify the joint distribution of $\{z(\mathbf{x}_0), \varepsilon(\mathbf{x}_0)\}$, assuming a normal random variable and prediction errors and conditional on the variance parameters of a geostatistical model. We also specify some x_0 which will give a conservative output-e.g. for a square grid we could specify x_0 at the centre of a grid cell where kriging variance is largest. From this it is possible to compute the conditional probability that $\tilde{Z}(\mathbf{x}_0) \ge z_t$ given that $z(\mathbf{x}_0) < z_t$, i.e. the probability, given that an intervention is required at \mathbf{x}_0 that, due to error in prediction, the mapped 120 variable does not show this. A detailed description of how the desired conditional probability can be obtained from the joint probabilities is presented in the Supplement.

2.3 Implicit loss function

The loss function is a function of the error of \tilde{Z} , the kriging estimate of Z, as an estimate of the true unknown value, z, $\mathcal{L}(\tilde{Z}-z)$. The loss function is explained in greater detail by Journel (1984), Goovaerts (1997) and Lark and Knights (2015). 125 Journel (1984) defined a general linear loss function as:

$$\mathcal{L}(\tilde{Z} - z) = \alpha_1 |\tilde{Z} - z| \text{ if } \tilde{Z} < z$$

= $\alpha_2 |\tilde{Z} - z| \text{ if } \tilde{Z} \ge z.$ (6)

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The parameters α_1 and α_2 have positive real values. The coefficient α_2 is the loss per unit error of underestimation and α_1 is the loss per unit of error of overestimation. The slopes, α_1 and α_2 define the asymmetry of the loss function. The loss function can be symmetrical, i.e. penalizing overestimation and underestimation equally; or can be asymmetrical because over-andunderestimation have different consequences. The asymmetry of the loss function is the ratio of the loss per unit value by which a quantity is underestimated to the loss per unit value of an overestimation (Lark and Knights, 2015). The asymmetry, a, is obtained by

$$135 \quad a = \frac{\alpha_2}{\alpha_1},\tag{7}$$

i.e., is independent of the absolute value of z. If the loss function depends only on the estimation error, then z can be set to zero, without loss of generality and the expected loss can be computed as a function of the error variance, and so of the sample size (Lark and Knights, 2015). Increasing sample size reduces the minimum expected loss in so far as it reduced the error variance. Therefore, the cost of obtaining n samples can be measured at which the marginal cost of additional sample point is equal to the reduction in expected loss that single sample achieves (Goovaerts, 1997). However, it maybe difficult to define

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a loss function prior to making decisions about sampling. The losses may not be easy to quantify, e.g. social costs of failing to intervene, costs of unnecessary interventions, loss of confidence in the decision-making organisation. Stakeholders can be helped to reflect on possible loss functions through the implicit loss function. It is a loss function that makes a specified sample





size, *n*, a rational choice, given the marginal costs. That is to say, it is the loss function implied by a choice of \bar{n} , assuming this 145 is rational. The implicit loss function is conditional on a logistic model, that expresses the marginal costs of sampling exercise and the conditional distribution of z as a function of effort (Lark and Knights, 2015) and is obtained by finding $\bar{\alpha}_1$ (given asymmetry), such that

$$\check{\mathcal{L}}(\bar{n}-1|\bar{\alpha}_1,\bar{\alpha}_2,\boldsymbol{\phi}) - \check{\mathcal{L}}(\bar{n}|\bar{\alpha}_1,\bar{\alpha}_2,\boldsymbol{\phi}) = \mathcal{C}(\bar{n}) - \mathcal{C}(\bar{n}-1), \tag{8}$$

where \bar{n} is the specified number of sample, C(n) is the function that returns the cost of *n* samples and ϕ is a vector of variogram parameters, so kriging variance is a contributor. The asymmetry can be set at different values, or inferred from other elicited opinions of the stakeholder group (Lark and Knights, 2015). The expected loss can be minimised at a location given some prediction distribution of \tilde{Z} for the variable of interest by specifying the value of variable corresponding to a given probability (P_0), i.e.,

$$\tilde{Z} = F^{-1}(P_0).$$
 (9)

155 Where, F^{-1} denote the quantile of the prediction distribution for a probability P_0 obtained from

$$P_0 = \frac{\alpha_2}{\alpha_1 + \alpha_2},\tag{10}$$

(Journel, 1984). Lark and Knights (2015) suggested that a stakeholder group might consider an implicit loss function for different \bar{n} as starting points in the elicitation of a sample size, or compare implicit loss function for different projects given different partitions of a total budget between them. No attempt has been made to elicit opinions from stakeholders on implicit loss function, so we tried it in this study.

2.4 Offset correlation

The expected correlation between the kriging predictions, $\tilde{Z}_1(\mathbf{x}_0)$, made from a square grid, of interval ζ , and predictions, $\tilde{Z}_2(\mathbf{x}_0)$, made from a second grid, a translation of the first grid by $\zeta/2$ in both directions is known as the offset correlation. The correlation of the two kriging predictions can be computed by:

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$$\rho_{\tilde{Z}_1,\tilde{Z}_2} = \frac{\mathbf{C}_{\tilde{Z}_1,\tilde{Z}_2}(\mathbf{x}_0)}{\sqrt{\sigma_{\mathbf{K}_{\tilde{Z}_1}}^2 \sigma_{\mathbf{K}_{\tilde{Z}_2}}^2}},\tag{11}$$

where $C_{\tilde{Z}_1,\tilde{Z}_2}(\mathbf{x}_0)$ is the covariance $\tilde{Z}_1(\mathbf{x}_0)$ and $\tilde{Z}_2(\mathbf{x}_0)$. $\sigma^2_{K_{\tilde{Z}_1}}$ and $\sigma^2_{K_{\tilde{Z}_2}}$ are the kriging variances of the predictions from the first and second grid, respectively.

The offset correlation depends on \mathbf{x}_0 , and is smallest at the location furthest from points on either grid. This minimum offset correlation is used to evaluate predictions from a grid spacing ζ . Offset correlation is bounded on the interval [0,1], which

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makes it intuitively easy to interpret as an uncertainty measure. As the uncertainty in the map, attributable to sample density, decreases, the offset correlation increases. The denser the grid the more consistent the maps and the offset correlation will be 1 if the maps are identical and 0 if they are entirely unrelated to each other. Lark and Lapworth (2013) describes the offset correlation in greater detail.





Materials and methods 3

175 **Basic approach** 3.1

We used the four methods, described above, to assess uncertainty in relation to sampling density, considering the problem of measuring a soil property relevant to crop management: soil pH, and a property of the crop: Segrain concentration. We used variograms from a national survey in Malawi for each variable (Gashu et al., 2021) to obtain sampling densities for further notional sampling for an administrative district in Malawi, Rumphi District, with an area of 4769 km². The outputs were

- presented to participants. The participants considered each method in turn and were asked to select a sampling grid density 180 based on the method. After doing this they were asked, for each method: Has the method helped you assess the implication of uncertainty in spatial prediction in as far as it is controlled by sampling? They were then asked: Which of these methods was easiest to interpret? Finally, the participants were asked to rank the method in terms of ease of use. Evaluation of the test methods were done using an online questionnaire on Microsoft Forms.
- The elicitation was conducted online using Zoom Video Communications (2022) in two sessions, 26th and 28th April 2022. 185 There were two sessions in order to accommodate participants from different time zones, and to manage the participants in smaller groups to allow for questions and feedback. The invited participants self-identified as (i) agronomist or soil scientist or (ii) public health or nutrition specialists. The participants also self-assessed their statistical/mathematical background and their frequency of use of statistics in their job role (perpetual, regular, occasional use).
- 190 We invited professionals working in agriculture, nutrition and health at civic organisations, universities, government departments from Ethiopia, Malawi and wider GeoNutrition sites (United Kingdom, Zambia and Zimbabwe). In total we had 26 participants (18 were agronomists or soil scientists and 8 public health or nutrition specialists). Ethical approval to conduct this study was granted by the University of Nottingham, School of Biosciences Research Ethics Committees (SBREC202122022FEO) and participants gave informed consent to their participation and subsequent use of their responses.
- 195 In the exercise, an introductory talk was given to explain the study's objectives. During the talk, we explained the four test methods (offset correlation, prediction intervals, conditional probabilities and implicit loss function) and how they can be used to assess the implications of uncertainty in spatial predictions to determine appropriate sampling grid space for a geostatistical survey. We explained the structure of the questionnaire to the participants. We emphasized to the participants that we were not testing their mathematical/statistical skills and understanding but rather were testing the accessibility of the methods using their responses. 200

Evaluation of the test methods was done through a questionnaire, as shown on Table 1. Using the first four questions, Q1 to Q4, we wanted to find out if the method helped to identify a sampling grid spacing. On Q5, we wanted the participants to assess the test methods in terms of their effectiveness in finding an appropriate grid spacing. We asked the participants to rank these methods in an order of their effectiveness, in their experience, and in terms of finding a level of uncertainty that they were

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able to tolerate when deciding about a sampling grid spacing. We asked them to put rank 1 as the most effective method and rank 4 the least.





Table 1. The list of questions used to elicit stakeholder opinions about the set of methods that can help end-users to assess the implications of uncertainty in spatial prediction in as far as this is controlled by sampling.

Number	Question	Response
Q1	We show you here some pairs of example maps of soil pH/Se _{grain} , each pair being based on a different grid spacing, and so with a different offset correlation. We also show scatter plots which illustrate the strength of the correlation. What do you think is the smallest correlation that would be acceptable if one of the maps were to be used to make decisions?	(1) 0.4 (2) 0.5 (3) 0.6 (4) 0.7 (5) 0.8 (6) 0.9
Q2	You are shown different scenarios for the prediction of soil pH/Se _{grain} from different grid spacings, which determine the width of the prediction interval. What is the grid spacing that gives the widest prediction interval that would be acceptable if one of the maps were to be used to make decisions?	 (1) Spacing=20km (2) Spacing=40km (3) Spacing=60km (4) Spacing=80km (5) Spacing=100km (6) Spacing=120km
Q3	At some location on the map the true value of soil pH/Se _{grain} indicates that an intervention is required, due to error in prediction there is a non-zero probability that the mapped soil pH/Se _{grain} does not show this, this probability increases with grid spacing as shown on the graph. What grid spacing do you think corresponds to the largest acceptable value of this probability?	 (1) Spacing=20km (2) Spacing=40km (3) Spacing=60km (4) Spacing=80km (5) Spacing=100km (6) Spacing=120km
Q4	We have three specified implicit loss functions for predictions Se _{grain} concentration over an area of 4,769 square kilometres (km ²) for a district/administrative region. With the implicit loss function we assume that the sample density is fixed (e.g. on budgetary grounds) and compute the loss function which would make that a rational choice. We then ask does the loss function implied by the decision look sensible?	(1) Spacing=10km(2) Spacing=20km(3) Spacing=40km
Q5	Please rank these methods in an order of their effectiveness, in your experience, in terms of finding a level of uncertainty that you are able to tolerate when deciding about a sampling grid density.	Rank 1 being MOST effective and Rank 4 the least

The offset correlation was the first method presented to the participants. This was followed by prediction intervals and conditional probabilities. The implicit loss function was the final method presented to the participants. We started with a measure we thought all our stakeholders would most easily understand and then moved on to the more complex methods.

210 **3.2 Test Methods**

3.2.1 Statistical modelling and spatial prediction of grain Se concentration and soil pH

the full data description is provided by Kumssa et al. (2022).

We used the data from a geostatistical survey conducted in Malawi for the GeoNutrition project (Gashu et al., 2021). Field sampling was undertaken to support the spatial prediction of micronutrient concentration in crops and soil across Malawi. Detailed description of soil and crop sampling in Malawi are presented by Gashu et al. (2021) and Botoman et al. (2022), and

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We undertook exploratory analysis of soil pH and Se_{grain} concentration using QQ plots, histograms and summary statistics to check whether there was need for transformation of the variables for the assumption of normality. The data for Se_{grain} concentration were skewed and it was necessary to transform them to natural logarithms. The variance parameters for both soil





pH and Se_{grain} concentration were estimated by residual maximum likelihood using the likfit procedure in the geoR packages (Diggle and Ribeiro, 2010) for the R platform (R Core Team, 2022) with a constant mean as the only fixed effect. These variance parameters were used in the subsequent test methods. The thresholds we considered, in this study for the prediction intervals and conditional probabilities were soil pH of 5 and Se_{grain} concentration of 38 µg kg⁻¹. The threshold for soil pH is 5 in Malawi, such that if the pH at a location falls below 5, it would be necessary to apply lime (Chilimba et al., 2013). The threshold Se_{grain} concentration is 38 µg kg⁻¹, such that a serving of 330g of grain flour provides a third of the daily estimated average requirement of Se_{grain} for an adult woman (Chagumaira et al., 2021). The intervention for soil pH was liming, and Se_{grain} was provision of fortified food.

3.2.2 Prediction intervals

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Using the variance parameters estimated in Section 3.2.1, we evaluated kriging variances at the centres of cells of square grids of different spacings. We considered minimum and maximum grid spacings of 0.05 and 125 km, respectively, with an increment of 0.5 km. We then computed the cell-centred block kriging variance the spacings we were considering by block kriging (Webster and Oliver, 2007). We considered different prediction for each variable but the prediction interval was fixed, depending only on grid spacing. The three predictions of soil pH were 4.8, 5.5 and 6.0 and those of Se_{grain} were 20, 55 and 90 μ g kg⁻¹. The predictions of soil pH and Se_{grain} concentration were presented to the participants in a chart.

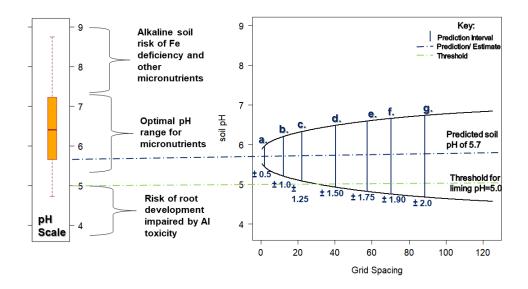


Figure 1. An example of a chart, for prediction intervals, with prediction of soil pH of 5.7 with prediction intervals and in relation to a threshold of pH = 5.0.





The chart consisted of (a) box plot of the distribution of the measured variable based on all soil samples from the study area, (b) a graph of the lower and upper prediction intervals for the prediction at the point of interest for grid spacings from 0 to 120 km, and lines indicating (c) the z_t and (d) the prediction (see Figure 1, S7 and S8). From the chart, we asked the participants to select the grid spacing that gives the widest prediction interval that would be acceptable if the mapped predictions were to be used to make decisions about soil management or interventions to address human Se deficiency.

3.2.3 Conditional probability

The conditional probability is a measure of uncertainty in terms of the risk of failing to intervene at some location given that an intervention is needed. We presented the participants with a chart of conditional probabilities plotted against grid spacing is shown on Figure 2 and Figure S9, and this probability increases with grid spacing. The conditional probability is bounded on an interval [0,1]. A probability of 1, indicates that the prediction will be equivalent to the overall mean of the dataset. If the prediction of Se_{grain} or pH was below the threshold, z_t , an intervention is needed. We then asked the participant at what grid spacing they thought corresponded to the largest acceptable value of this probability.

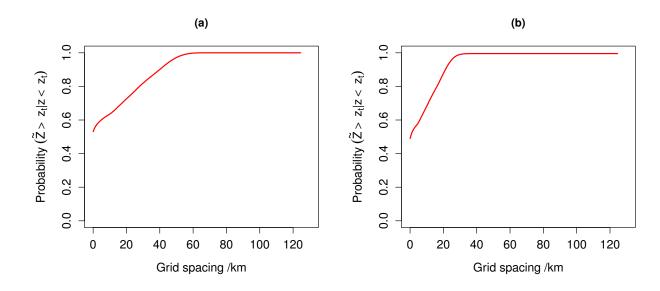


Figure 2. An example of the chart of conditional probabilities plotted against grid spacing for (a) soil pH and (b) Se_{grain} concentration. At a location \mathbf{x}_0 , \tilde{Z} is the prediction and z is the value of the variable at that location.

3.2.4 Implicit loss functions

In order to compute the implicit loss function, we needed a cost model for Rumphi district. We used the function defined in Lark and Knights (2015) to return the costs of n samples over an area $A \text{ km}^2$, i.e. a sample density of r = N/A samples per km²:





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$$C(n) = \omega + vAr + \beta At_r,$$
 (12)

where ω are the fixed costs, v cost of laboratory analysis per unit, and β the field costs per work day per team. The quantity t_r is time taken to sample per km² at a density of r per km². We obtained these costs for Rumphi district by considering the available costs for crop sampling during the GeoNutrition survey conducted in Malawi at national-scale (Gashu et al., 2021; Kumssa et al., 2022). A detailed description of how the costs were computed is presented in the Supplementary Material.

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We fixed the asymmetry ratio at 1.5, assuming the elicited mean probability threshold from similar stakeholders in Ethiopia and Malawi (Chagumaira et al., 2022) can be regarded as an approximation of P_0 which corresponds to a quantile of prediction distribution. This implied a bigger loss for overestimation of the variables (i.e. failing to intervene of Se_{grain} are smaller than prediction). With the implicit loss function we assumed that the sample density is fixed (e.g. on budgetary grounds) and computed the loss function which would make that a rational choice. We presented three specified implicit loss functions for predictions of Se_{grain} for Rumphi district, with an area of 4,769 km² with sampling densities fixed at 10, 20 and 40km. Figure 3 and Figure S10, shows the implicit loss function for Se_{grain}. We then asked the participants to identify the loss

function implied by the sampling decision that looked more plausible to make decisions about interventions to address human

Se deficiency.

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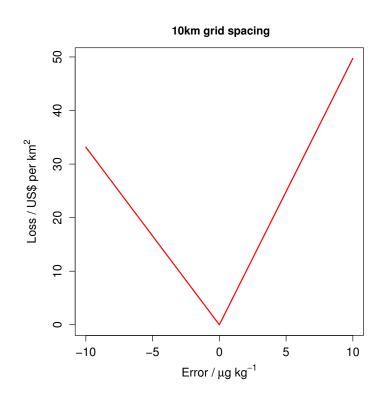


Figure 3. An example of specified implicit loss functions for predictions of Segrain concentration at a 10km grid spacing.





3.2.5 Offset Correlation

We presented the participants with pairs of example maps of soil pH and Se_{grain} concentration, each pair being based on a different grid spacing, and so with different offset correlation. We also showed scatter plots that illustrated the strength of the correlation. Figure 4, shows an example of pairs of maps of Se_{grain} concentration and the corresponding scatterplot (see Figure S5 and S6). The correlation plots showed the kriging predictions for soil pH and Se_{grain} concentration predicted with parameters estimated in Section 3.2.1. We asked the participants the smallest offset correlation that would be acceptable if one of the maps were to be used to make decisions based on the soil or grain property.

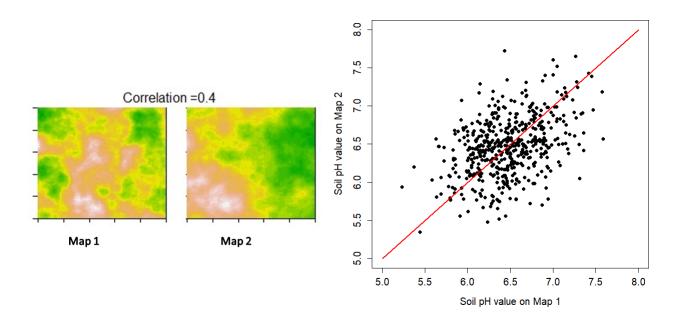


Figure 4. The pairs of example maps of Segrain concentration and corresponding scatterplot for offset correlation 0.4.

3.3 Data Analysis

3.3.1 Test methods

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The results for Q1 to Q4 were presented as contingency tables. The rows of each table correspond to the response (e.g. the different grid spacings) and, the full table, the columns correspond to the frequency of use of statistics, nested, within professional group and nested within variable used (soil pH or Se_{grain}). Contingency tables allowed us to test the null hypothesis of random association of responses with the different factors in the columns. The expected number of responses under the null hypothesis, $e_{i,j}$ in a cell [i, j], is a product of row (n_i) and column (n_j) totals dived by the total number of responses (N), and





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this the null hypothesis of the contingency table which is equivalent to an additive log-linear model of the table. An alternative to the additive model for the contingency table, is the saturated model that has an extra $(n_r - 1)(n_c - 1)$ term that allows for interaction amongst the columns and tables of the table. The proportions of observed responses $o_{i,j}$ may differ from $e_{i,j}$ in a cell [i, j] and the likelihood ratio statistic or deviance, L, can be used to provide evidence against the null hypothesis. The likelihood ratio statistic is computed by

$$L = 2\sum_{i=1}^{N} \sum_{j=1}^{N} o_{i,j} \log \frac{o_{i,j}}{e_{i,j}}.$$
(13)

where L has an approximate χ^2 distribution under the null hypothesis of random association between the rows and columns of the table, with $(n_r - 1)(n_c - 1)$ degrees of freedom (Christensen, 1996; Lawal, 2014). We fitted the log-linear models using the logIm function from the MASS package (Venables and Ripley, 2002) for the R platform.

A contingency table can be partitioned to evaluate whether there are differences in the responses of the participants based on (i) variable used in the test method, (ii) professional group and (iii) by frequency of use of statistics. In Table 2, we illustrate how the contingency table can be partitioned. The table can be partition into components corresponding to pooled table and subtables of the full table.

The full table in Table 2, was partitioned into subtables for soil pH (Subtable 1 in Figure 3), and Se_{grain} concentration (Subtable 2 in Table 2). Then the pooled table completes the partition. The degrees of freedom and deviances for the three table sum to the degrees of freedom and deviance of the full table. Using the contingency table, we could conclude if there are differences in responses for the two variables. The full table in can further be partitioned, in a similar way, by the background of the respondents i.e., professional group and frequency of use of statistics.

In our study, we wanted to find out if the responses recorded by the stakeholders depended on the variable used (soil pH or Se_{grain} concentration), and background of the respondent. We expected the responses to differ. We thought the stakeholders would have different perceptions of the impacts of the uncertainty for soil pH and Se_{grain} concentration. There were more agronomist or soil scientists than public health or nutrition specialists in the meeting, and we expected the priorities of the groups to differ when making interventions for soil pH and Se_{grain} concentration. We also thought the frequency of use of statistics would influence the choice of method used to select an appropriate grid spacing.

We first tested for differences responses recorded for each test method, by the variable used (soil pH or Se_{grain} concentration) using contingency tables. The responses from stakeholders in different professional groups were pooled within the two variables, as illustrated by the Pooled table 1 on Table 2. This gave us a six (responses) by two (variables) contingency table

305 with 5 degrees of freedom for the questions corresponding to offset correlation, prediction intervals and conditional probabilities (Q1 to Q3). However, for the implicit loss function we did not consider this because we only had a loss function for Se_{grain} concentration.

Second, we considered if the differences in the responses depended on the professional group of the respondent. Finally, we considered whether the frequency of use of statistics in their job role had an impact on the responses recorded by the

310 respondents. For some questions, we noted differences in the responses when pooled within variable used (soil pH or Se_{grain} concentration) and there was no differences in responses in professional groups and frequency of use of statistics for all

Table 2. An illustration of how the log-likelihood ratio was used to partition full table into subtables and pooled tables.

Deviance = L₁ Response = O_U Accross of freacham = DE = (2-4)-(42-4) =

	ке deg	Response = O _{ij} degrees of freedom =		<i>DF</i> _F = (2–1)×(12–1) = 11) = 11								
				Soil pH	рН					Segrain concentration	centration		
		Agronomy or soi	or soil scier	il science (AGS)	Public heal	Public health or nutrition (PHN)	on (PHN)	Agronomy	Agronomy or soil science (AGS)	ice (AGS)	Public hea	Public health or nutrition (PHN)	on (PHN)
Full table	Response	Occasionally Reg	Regularly	ularly Perpetually	Occasionally	Regularly	Perpetually	Occasionally Regularly Perpetually Occasionally Regularly Perpetually	Regularly	Perpetually	Occasionally Regularly Perpetually	Regularly	Perpetually
	Spacing 1	01,1	01,2	0 _{1,3}	0 _{1,4}	0 _{1,5}	0 _{1,6}	01,7	0 _{1,8}	0 _{1,9}	0 _{1,10}	0 _{1,11}	O _{1,12}
	Spacing 2	0 _{2,1}	0 _{2,2}	0 _{2,3}	O _{2,4}	0 _{2,5}	0 _{2,6}	$O_{2,7}$	0 _{2,8}	0 _{2,9}	O _{2,10}	0 _{2,11}	O _{2,12}
		_ •	Pooled table	؛ (Professiona)	Pooled table (Professional groups pooled within variable):	∋d within va	riable):			I	<u> </u>		
		_ •	degrees of fi	reedom = <i>DF</i> _P ,	degrees of freedom = $DF_{P_1} = (2-1)\times(2-1) = 1$	= 1							
			Response	So	Soil pH	Sear	Segrain concentration	ion					
	↓ Poo	Pooled table 1		0 _{1,1} +0 _{1,2} +0 _{1,3}	$O_{1,1} + O_{1,2} + O_{1,3} + O_{1,7} + O_{1,8} + O_{1,9} = O_{1,4} + O_{1,5} + O_{1,6} + O_{1,10} + O_{1,11} + O_{1,12}$	0 _{1,4} +0 _{1,5} +	-0 _{1,6} +0 _{1,10} +0 ₁	,11+0 _{1,12}					
			Spacing 2	U _{2,1} +U _{2,2} +U _{2,3}	$O_{2,1}+O_{2,2}+O_{2,3}+O_{2,7}+O_{2,8}+O_{2,9} O_{2,4}+O_{2,5}+O_{2,6}+O_{2,10}+O_{2,11}+O_{2,12}$	02,4+02,5+	-0 _{2,6} +0 _{2,10} +0 ₂	,11+O _{2,12}					
			Subtable 1 (Soil pH): Deviance= L _{s1} degrees of freedom =	Soil pH): st reedom = <i>DF</i> _{St}	Subtable 1 (Soil pH): Deviance= L _{s1} degrees of freedom = DF _{S1} = (2-1)×(6-1) = 5	ء ت							
						Soi	Soil pH				Devi	Deviance partition:	:u
				Agronom	Agronomy or soil science (AGS)	e (AGS)	Public h	Public health or nutrition (PHN)	on (PHN)			Lr=Ln+L_1+L_2	
	Sub;	Subtable 1	Response	Occasionally	Occasionally Regularly Perpetually	erpetually	Occasionally	Regularly	Perpetually			5	
			Spacing 1	01,1	0 _{1,2}	0 _{1,3}	0 _{1.4}	0 _{1,5}	0 _{1,6}		Degr	Degrees of freedom	om
			Spacing 2	02,1	O _{2,2}	O _{2,3}	0 _{2,4}	O _{2,5}	0 _{2,6}			DF _f =DF _{p1} +DF _{s1} +DF _{s2}	DF _{s2}
			Subtable 2 (Se Deviance – I	Subtable 2 (Se _{grain} concentration): Deviance - I	ntration):								
			degrees of	freedom= <i>DF</i> _S	degrees of freedom= $DF_{S2} = (2-1)\times(6-1) = 5$	= 5							
						Se _{grain} con	Segrain concentration						
				Agronomy	Agronomy or soil science (AGS)	e (AGS)	Public h	Public health or nutrition (PHN)	on (PHN)				
	tis:	Subtable 2	Response	Occasionally	Occasionally Regularly Perpetually	^o erpetually	Occasionally	Regularly	Perpetually				
	;		Spacing 1	0 _{1,7}	0 _{1,8}	0 _{1,9}	0 _{1,10}	O _{1,11}	0 _{1,12}				





O_{2,12}

0_{2,11}

0_{2,10}

02.9

0_{2,8}

02.7

Spacing 2





questions. We further analysed the pooled tables or separate subtables to examine if the responses where uniformly distributed and the null hypothesis is a random distribution. We wanted to test whether the responses of the participants were uniform, i.e., each grid spacing has equal likelihood of occurrence.

315 3.3.2 Assessment of the method

The responses for the Q5 were tabulated with the methods as the columns and ranks as the rows. The participants ranked their preferred method first. However, in our analysis we reversed the order by assigning a score of 4 for the most preferred method and 1 for the least. We computed the mean ranks, \bar{r}_i , for each method for all respondents. We then separated the respondents by their professional group and computed the mean ranks.

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6 Finally we separated the respondents by their frequency of use of statistics in their job role. Under a null hypothesis of random ranking for set of k ranks, the expected mean rank is (k+1)/2. The evidence against this hypothesis is measured a statistic distributed as $\chi^2(k-1)$:

$$\frac{12n}{k(k+1)}\sum_{i=1}^{k} \left\{ \bar{r}_i - \frac{k+1}{2} \right\},\tag{14}$$

where n is the total number of rankings (Marden, 1996).

325 4 Results

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4.1 Test methods

4.1.1 Method 1: Offset correlation

The full table for Q1 and the subsequent subtables are presented in the Appendix of the paper (Tables A1–A3). There were no differences in the responses of the when the columns were pooled by the variable used, soil pH vs. Se_{grain} concentration, p = 0.656 (Table 3).

There were no differences in the responses when the columns were also pooled within professional groups (p = 0.491) and frequency of use of statistics (p = 0.595). Further analysis of the question on offset correlation was based on pooled counts, see Table A3. There was strong evidence to reject the null hypothesis that the responses are uniformly distributed (p = 0.003). Figure 5 shows the responses of how all the participants responded to Q1, for offset correlation.

- 335 Most of the respondents selected offset correlation of 0.7 as the smallest offset correlation that would be acceptable if one of the maps were to be used to make decisions based on the soil or grain property. We extracted the grid spacings, for soil pH and Segrain, corresponding to the selected offset correlation of 0.7. The spacings were extracted from a plot of offset correlation against grid spacing obtained from the variance parameters of each variable (see Figure S4). The grid spacing for soil pH is 25 km and for Segrain is 12.5 km. The grid spacing corresponding to the offset correlation for each variable were computed from
- 340 the variogram of the variable.





Table 3. Analysis of the question on offset correlation, Q1, according to variable used, professional group and frequency of use of statistics.

	Deviance (L^2)	Degrees of freedom	P
Full contingency table analysis			
Full table	54.57	55	0.491
Pooled by variable used (pH v. Se_{grain})	3.29	5	0.656
Pooled by professional group	6.50	5	0.260
Pooled by frequency of use of statistics	8.35	10	0.595
Subtable-pooled counts: variable used			
Soil pH	27.01	25	0.352
$\mathrm{Se}_{\mathrm{grain}}$	24.2	25	0.50
Subtable-pooled counts: professional group			
Agronomist or soil scientist	26.25	25	0.394
Public health or nutrition specialist	21.81	25	0.64
Subtable-pooled counts: frequency of use of statistics			
Perpetual use of statistics	8.99	15	0.87
Occasional use of statistics	18.17	15	0.254
Regular use of statistics	19.06	15	0.21
Subtable-pooled counts			
Responses are uniformly distributed	17.69	5	0.003

4.1.2 Prediction interval

There were no differences in the responses when pooled within the variable used, p = 0.656, for prediction intervals (Table 4). We then pooled the responses within the professional groups, and there was no evidence to reject the null hypothesis (p = 0.498). Also, there were differences when responses were pooled within frequency of use of statistics, p = 0.152. Therefore,
further analysis of the question on prediction intervals was based on pooled counts of responses. There was no evidence to reject the null hypothesis that the responses are uniformly distributed (p = 0.169). Figure 6 shows the bar charts of how all the participants responded to the Q2 for prediction intervals. For this method, there no clear choice of grid spacing for sampling for soil pH and Segrain.

4.1.3 Conditional probabilities

Table 5 shows the results for partitioning the contingency table for the question on conditional probabilities, Q3. There was strong evidence to reject the null hypothesis when the columns were pooled by variable used, $p \le 0.001$. Therefore, further analysis was based on separate subtables for soil pH and Se_{grain} concentration. For both variables, there were no differences





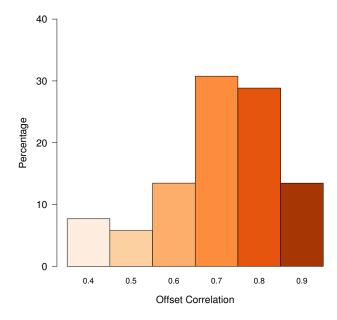


Figure 5. Bar charts showing how the participants responded to Q1 for offset correlation.

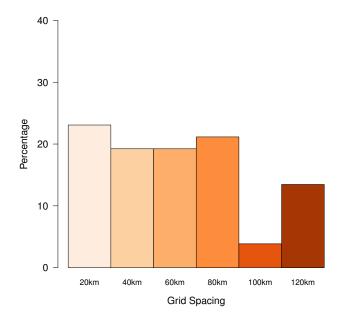


Figure 6. Bar charts showing how the participants responded to the Q2 for prediction intervals.





Table 4. Analysis of the question on prediction interval, Q2, according to variable used, professional group and frequency of use of statistics.

	Deviance (L^2)	Degrees of freedom	P
Full contingency table analysis			
Full table	56.0	55	0.437
Pooled by variable used (pH v. Se_{grain})	0.972	5	0.965
Pooled by professional group	4.36	5	0.498
Pooled by frequency of use of statistics	14.5	10	0.152
Subtable-pooled counts: variable used			
Soil pH	23.8	25	0.531
${ m Se}_{ m grain}$	31.2	25	0.181
Subtable-pooled counts: professional group			
Agronomist or soil scientist	26.5	25	0.381
Public health or nutrition specialist	25.1	25	0.455
Subtable- pooled counts: frequency of use of statistics			
Perpetual use of statistics	9.68	15	0.840
Occasional use of statistics	16.88	15	0.330
Regular use of statistics	15.08	15	0.450
Subtable- pooled counts			
Responses are uniformly distributed	7.77	5	0.169

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in the responses when the columns were pooled within professional groups and frequency of use of statistics. For soil pH there was strong evidence to reject the null hypothesis that the responses are uniformly distributed ($p \le 0.001$). A similar result was found for Se_{grain} concentration ($p \le 0.001$). The bar charts for the responses for the question on conditional probabilities for soil pH are presented in Figure 7a. The grid spacing chosen by the participants for soil pH is 60 km. The responses for Se_{grain} concentration are presented in Figure 7b. The grid spacing made was 40 km.

4.1.4 Implicit loss functions

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The results for partitioning the contingency table for implicit loss function, Q4, are presented in Table 6. There were no differences in the responses when the columns of the table were pooled within professional groups (p = 0.781) and frequency of use of statistics (p = 0.828). Further analysis of the question on implicit loss function was based on pooled counts of responses. There was strong evidence to reject the null hypothesis that the responses are uniformly distributed ($p \le 0.001$). The bar charts for the responses pooled counts for all respondents are shown on Figure 8. The grid spacing chosen by the participants for Se_{grain} concentration is 20 km.





Table 5. Analysis of the question on conditional probabilities, Q3, according to variable used, professional group and frequency of use of statistics.

	Deviance (L^2)	Degrees of freedom	P
Full contingency table analysis			
Full table	60.6	55	0.281
Pooled by variable used (pH v. Se_{grain})	26.7	5	< 0.001
Pooled by professional group	5.32	5	0.378
Pooled by frequency of use of statistics	14.5	10	0.152
Subtable-pooled counts: variable used			
Soil pH	12.1	25	0.986
$\mathrm{Se}_{\mathrm{grain}}$	21.8	25	0.647
Soil pH subtable-pooled counts: professional group			
Pooled within professional group	4.48	5	0.483
Agronomist or soil scientist	3.10	10	0.979
Public health or nutrition specialist	4.50	10	0.922
Soil pH subtable-pooled counts: frequency of use of statistics			
Pooled within frequency of use of statistics	0.889	10	1.00
Perpetual use of statistics	4.50	5	0.480
Occasional use of statistics	4.36	5	0.499
Regular use of statistics	2.33	5	0.802
Soil pH subtable-pooled counts			
Responses are uniformly distributed	50.15	5	< 0.001
$\mathrm{Se}_{\mathrm{grain}}$ subtable–pooled counts: professional group			
Pooled within professional group	4.77	5	0.445
Agronomist or soil scientist	11.0	10	0.361
Public health or nutrition specialist	6.09	10	0.808
$\mathrm{Se}_{\mathrm{grain}}$ subtable–pooled counts: frequency of use of statistics			
Pooled within frequency of use of statistics	9.55	10	0.481
Perpetual use of statistics	1.73	5	0.886
Occasional use of statistics	5.55	5	0.353
Regular use of statistics	4.99	5	0.417
$\mathrm{Se}_{\mathrm{grain}}$ subtable–pooled counts			
Responses are uniformly distributed	36.77	5	< 0.001





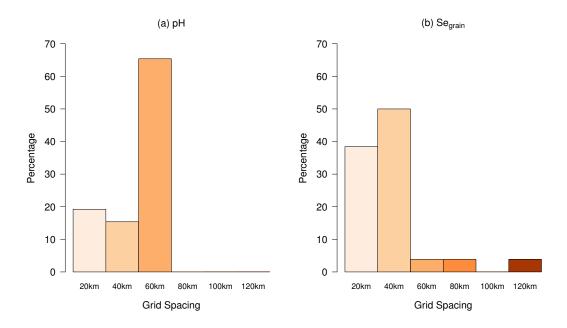


Figure 7. Bar charts showing how all the participants responded to the Q3 for conditional probabilities for (a) soil pH and (b) Se_{grain} concentration.

365 4.2 Assessment of the test methods

The question on ranking of the method was analysed in three ways. At first we computed the mean ranks for all participants and tested for the evidence against the null hypothesis of random ranking. There is strong evidence to reject the null hypothesis of random ranking, $p \le 0.001$ (Table 7). Then the mean ranks were computed for each professional group and there was strong evidence to reject the null hypothesis of random ranking in each group ($p \le 0.001$). Finally, we separated the participants into three groups according to their frequency of use of statistics in the job role, and computed the mean ranks in each group. There was strong evidence to reject the null hypothesis of random ranking in each group ($p \le 0.001$).

The offset correlation was ranked as the most effective by all respondents (Figure 9a) and implicit loss function as the least effective. Both professional groups (i.e. agronomist or soil scientist and public health or nutritionist) ranked offset correlation first but differed in the second and least ranked methods (Figure 9b to 9c). Public health or nutrition specialists ranked second prediction intervals and implicit loss function as the least effective. The agronomist or soil scientist group ranked prediction

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intervals as the least effective and conditional probabilities as second.

When respondents were separated by their frequency of use of statistics, offset correlation was also ranked first (Figure 9d to 9f). Those who use statistics occasionally, in their job role, ranked the implicit loss function as the second best and the prediction intervals the least. Conditional probabilities were ranked second and implicit loss function as the least effective by





Table 6. Analysis of the question on implicit loss function, Q4, according to variable used, professional group and frequency of use of statistics.

	Deviance (L^2)	Degrees of freedom	Р
Full contingency table analysis			
Full table	8.91	10	0.541
Pooled by professional group	0.49	2	0.781
Pooled by frequency of use of statistics	1.49	4	0.828
Subtable-pooled counts: professional group			
Agronomist or soil scientist	2.33	4	0.676
Public health or nutrition specialist	6.09	4	0.193
Subtable- pooled counts: frequency of use of statistics			
Perpetual use of statistics	1.73	2	0.422
Occasional use of statistics	1.73	2	0.422
Regular use of statistics	3.96	2	0.138
Subtable- pooled counts			
Responses are uniformly distributed	54.00	2	< 0.001

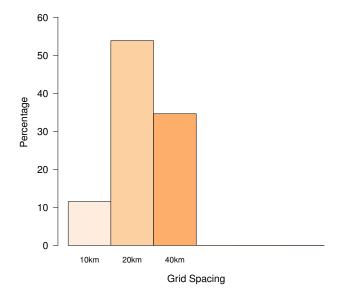


Figure 8. Bar charts showing how all the participants responded to the Q4 for implicit loss function.





Table 7. Analysis of Q5 according to professional group and level of use of statistics in job role

	Test Statistic (X^2)	Degrees of freedom	P^*
All respondents	61.1	3	< 0.001
Professional group			
Agronomist or soil scientist	49	3	< 0.001
Public health or nutrition specialist	15.6	3	< 0.001
Frequency of use of statistics			
Perpetual user of statistics	34	3	< 0.001
Occasional user of statistics	28.5	3	< 0.001
Regular user of statistics	49.8	3	< 0.001

380 those who regularly use statistics in the job role. Those who use statistic at all times, ranked conditional probabilities second. Prediction intervals and implicit loss functions were ranked last.

5 Discussion

In this study, we presented to groups of stakeholders, four methods (offset correlation, prediction intervals, conditional probabilities and implicit loss functions) that can be used to support decisions on sampling grid spacing for a survey of soil pH and 385 Se_{grain}. We wanted to find out if the stakeholders had a preference among the approaches presented to them. Offset correlation was ranked first as the method the stakeholders found easy to interpret (see Figure 9), and over 70% of the stakeholders specified a correlation of 0.7 or more as a criteria for adequate sampling intensity. During the feedback session, stakeholders highlighted that they were more familiar with the concept of correlation, with a closed interval of [0,1]. This explains why there more consistent responses under this method. Our results are consistent with findings of Hsee (1998), that relative measures of some uncertain quantity (Hsee gives an example of the size of a food serving relative to its container) are more readily evaluated than absolute measures (the size of serving). An easy-to-evaluate attribute, such as the bounded correlation of [0,1], has a greater impact on a person's judgement of utility. Hsee (1998) describe this as the "relation-to-reference" attribute. It is therefore, not surprising that the offset correlation is highly-ranked.

The offset correlation will be more useful for stakeholders who are not able to express their quality requirement for information in terms of quantities such as kriging variance. Furthermore, it is an intuitively meaningful measure of uncertainty, it recognises that spatial variation means that maps interpolated from offset grids will differ but that the more robust the sampling strategy the more consistent they will be. There is a paradox here, however, in that the previous study Chagumaira et al. (2021) showed that interpretation of survey outputs in terms of uncertainty was easiest for stakeholders with measures related directly to a decision made with the information. The offset correlation is a general measure, and the absolute magnitude of uncertainty





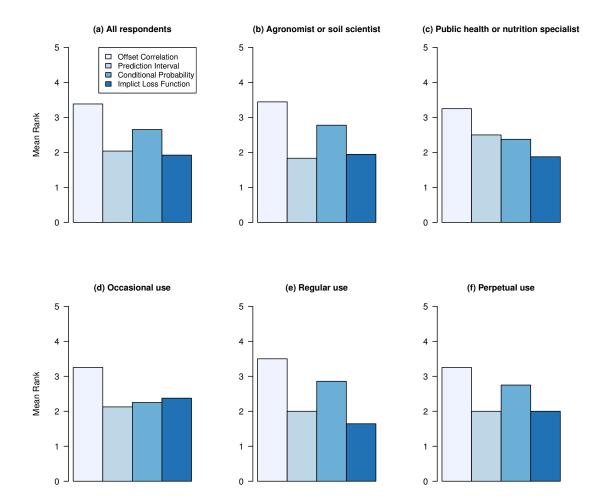


Figure 9. Ranking of test methods in terms on the most effective: (a) by all respondents, professional group: (b) agronomists or soil scientist and (c) public health or nutritionist specialists, and frequency of use of statistics: (d) occasional use, (e) regular use and (f) perpetual use.





400 has greater bearing on a specific decision. Indeed, Lark and Lapworth (2013) proposed the offset correlation particulary with general baseline surveys in mind. There is more research needed to develop sound but accessible ways to engage stakeholders with uncertainty consistent across planning and interpretation.

All the stakeholders ranked conditional probabilities second. Under this method, the stakeholders selected spacings where conditional probabilities was 1.0 or very close, i.e. the prediction equivalent to the overall mean. This suggest that the stake-

- 405 holders may not have fully understood the method. This finding is consistent with the general view that users of information commonly find probabilities difficult to interpret (Spiegelhalter et al., 2011). Because probabilities are bounded [0,1], the 'relation-to-reference' attribute effect by Hsee (1998) may explain the previous preference for conditional probabilities (Jenkins et al., 2019; Chagumaira et al., 2021), but stakeholders still struggle to interpret them correctly. Perhaps if the problem had been framed in a different way, the stakeholders may have understood this method much better. More work is needed to in-
- 410 vestigate if framing the conditional probabilities in a different way would improve the judgement of utility of the stakeholders. More examples and more illustration may be needed in order to 'prime' the participants before the exercise.

Prediction intervals were ranked third by all the respondents, but there was no evidence against the null hypothesis of random selection among the available spacings. During a feedback session, the stakeholders cited difficulties of assessing the significance of a given prediction interval given that it can be associated with different prediction values. For very large or small

415 prediction values the uncertainty is immaterial, it is near decision threshold that it becomes important. Similarity, prediction intervals were not highly ranked by stakeholders for communicating uncertainty in maps (Chagumaira et al., 2021). Similar reasons were given the respondents. We expected that prediction intervals to be of greatest value for specific interpretation of particular sites, but would be of limited value for survey planning.

The implicit loss functions was the lowest-ranked method. The group also commented that they had difficulties understanding this method, and most people opted for the central value. Loss functions are not readily accessible. It is difficult to define a loss function because it requires the cost of the errors, and we tried to show stakeholders some consistent approach with some plausible design. The fact that they did not understand the loss functions, shows there is need for more specific examples to help stakeholders think about loss function and their implications. It might help the stakeholders to provide some quantitative information about the costs of the survey, cost associated with intervention campaigns and costs of the impacts on MNDs on a

425 country's gross domestic production. A reflection of these would allow the stakeholder to use these implicit assumptions when they were making decisions for selecting a fixed grid spacing for working with (Lark and Knights, 2015).

The background of the stakeholders, i.e., professional group and frequency of use of statistics, had no influence on their responses for all the methods. However, the background of the stakeholders had an influence on their ranking of the methods in terms of their effectiveness. The offset correlation was ranked as the most effective by all professional groups and by all respondents separated by frequency of use of statistics. Prediction intervals were ranked least effective by those respondents who identified as agronomist or soil scientist, but were ranked second by those in public health or nutrition.

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At the begin of the online workshop, we explained each method with the aid of illustrations. After an explanation each method, there was a feedback session to allow the participants opportunities to seek clarity on ambiguous and unfamiliar concepts from the presenters. The participants' questions were answered and explained in different ways by CC, RML and





AEM, with the use of illustrations. However, there are limitations with online workshops. Most participants would have the cameras switched off, and the "unconscious" feedback to presenters by observing the reactions of participants could not be noticed as during in-person workshops. The "unconscious" feedback would prompt the presenter to use a different approach to explain unfamiliar concepts and ambiguous terms. Due to internet connectivity, online workshops are timed and there will less time for feedback sessions. In such instances, respondents may seek clarity from the colleagues who have the same interests, resulting in bias (Ball, 2019).

All the methods may give different result.

All the methods may give different results for different variable, because they depend on the variogram of the variable in question. There maybe different grid spacings selected for the different variables. A potential problem may exist, if the variables were to be sampled in one survey and what spacing should be used? This is an important question that needs to be addressed when planning for soil and crop sampling. It may be reasonable to opt for the grid spacing for the variable that maybe the hardest to characterise. Another option would to consider some minimum quantile over all variables through a group elicitation. Black et al. (2008) proposed that a critical subset of soil properties are identified such that the overall sampling scheme is satisfactory for all of the so-called 'canary indicators'.

6 Conclusions

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Users of information on soil variation need accessible ways of understanding the implications of sampling designs on spatial prediction and their uncertainties. The background (professional group and frequency of use of statistics) of the stakeholder had no influence in the responses selected for each approach. Of these methods we tested, the offset correlation was most favoured, but had no direct link to decision making and some methods of communication were not well understood (conditional probabilities and implicit loss functions). The offset correlation will likely be more useful to stakeholders, with little or no statistical background, who are unable to express their requirements of information quality based on other measures of uncertainty. Although previous work has found that uncertainty of spatial information is best understood when presented in terms of a decision-specific metric, that was not the case here. This shows that more work must be done to develop and elucidate decision specific approaches, perhaps through methods to elicit useful loss functions.

Appendix A

460 In this appendix, we present the full contingency table for Q1, for offset correlation, is presented as Table A1, in the appendix. The table shows how many individuals selected the given responses for offset correlation. This table is according to variable used (soil pH vs. Se_{grain}), professional group and frequency of use of statistics. Table A2 shows how many individuals selected a given response to Q1, for offset correlation, when columns are pooled within variable used, soil pH or Se_{grain} concentration. Table A3 shows the pooled counts of the responses for Q1.



according to variable used, professional group and frequency of use of statistics in job role. The figures in parentheses are the expected numbers, $e_{i,j}$ a product of Table A1. The full contingency table for Q1 for offset correlation, showing how many respondents selected the given responses for offset correlation. The table is row and column totals dived by the total number of responses. The acronyms represent the professional groups (AGS-agronomist or soil scientist; PHN- public health or nutrition specialists), and frequency of use of statistics in job role (Pep- perpetual use of statistics; Occ-Occasional use of statistics and Reg- regular use of statistics).

 $\mathrm{Se}_{\mathrm{grain}}$

soil pH

Response

AGS PHN	Pep Occ Reg Pep Occ Reg	0(0.23) $2(0.31)$ $1(0.31)$ $0(0.08)$ $0(0.31)$ $0(0.23)$	(0.17) $0(0.23)$ $1(0.23)$ $0(0.06)$ $0(0.23)$ $0(0.17)$	(0.40) 1(0.40) 0(0.54) 0(0.54) 0(0.13) 1(0.54) 2(0.40)	31)	29) 1(1.15)	
	Reg	0(0.23) 0(0.	1(0.17) 0(0.	0(0.40) 1(0.	2(0.92) 1(0.	0(0.87) 0(0.	
NHA	Occ	0(0.31) 0	0(0.23) 1	l(0.54) C	3(1.23) 2	\circ	
	Pep	0(0.08)	0(0.06)	0(0.13)	0(0.31)	1(0.29)	
	Reg	1(0.85)	1(0.23) 0(0.63)	(1.48)	(3.38)	5(3.17)	
AGS	Occ	0(0.31)	1(0.23)	0(0.54) 1	2(1.23)	0(1.15)	
	Pep	0(0.23)	0(0.17)			0(0.87)	
		Offset=0.4 0(0.23)	Offset=0.5 0(0.17)	Offset=0.6 1(0.40)	Offset=0.7 1(0.92)	Offset=0.8 0(0.87)	







Table A2. A subtable showing how many individuals selected a given response to Q1, for offset correlation, when columns are pooled within variable used (soil pH vs. Se_{grain} concentration).

Response	soil pH	$\mathrm{Se}_{\mathrm{grain}}$
Offset=0.4	1	3
Offset=0.5	2	1
Offset=0.6	3	4
Offset=0.7	10	6
Offset=0.8	6	9
Offset=0.9	4	3

Table A3. Pooled responses given to the question on offset correlation.

Pooled counts
4
3
7
16
15
7





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Competing interests. The authors declare that they have no conflict of interest.

Disclaimer. The funders were not involved in the design of this study or the collection, management, analysis and interpretation of the data, the writing of the report or the decision to submit the report for publication.

470 *Ethics statement.* Ethical approval to conduct this study was granted by the University of Nottingham, School of Biosciences Research Ethics Committees (SBREC202122022FEO) and participants gave informed consent to their participation and subsequent use of their responses.

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